

# **SOLUTIONS**

## **WEEKLY TEST-11**

**GZRA-1901, GZR-1901( $\alpha$ )**

**GZRS-1901**

**(JEE ADVANCED PATTERN)**

**Test Date: 03-09-2017**



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## CHEMISTRY

1. (B)

Chromium

2. (C)

$$PV_1 = n_1RT$$

$$PV_2 = n_2RT$$

$$\text{or, } P(V_2 - V_1) = (n_2 - n_1)RT$$

$$\text{or, } \frac{0.0821 \times 50}{1000} = (n_2 - n_1) \times 0.0821 \times 350$$

$$\text{or, } n_2 - n_1 = \frac{1}{7000} \text{ mole} = \frac{1}{7} \text{ m.mole}$$

3. (B)

$$\frac{1}{2}mv^2 = \frac{KQ_1Q_2}{x}$$

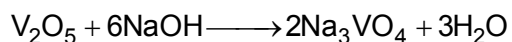
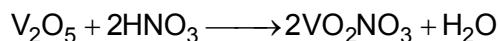
$$\text{or, } x \propto \frac{Q_2}{V^2}$$

$$\text{So, } \frac{x_1}{x_2} = \frac{40 \times 4V^2}{V^2 \times 80} = 2:1$$

4. (C)

$$Z_{\text{eff}} \propto \frac{1}{\text{size}}$$

5. (A)



Amphoteric oxide can react with both acid and base.

6. (D)

Enthalpy of dissociation is endothermic process.

7. (D)

$$\text{Initially, } P_{\text{Ne}} = \frac{3}{5} \times 200 = 120 \text{ torr}$$

In final condition, gases present are Ne and H<sub>2</sub>O(g)

$$P_{\text{Ne}} = 120 \times 2 = 240 \text{ torr} \left[ P \propto \frac{1}{V}, n, T \text{ constant} \right]$$

$$P_{\text{H}_2\text{O(g)}} = 50 \text{ torr} \text{ [Aqueous tension]}$$

$$P_{\text{total}} = 290 \text{ torr}$$

8. (A), (C)

(B)  $F_{(\text{aq.})}^- < Cl_{(\text{aq.})}^- < Br_{(\text{aq.})}^- < I_{(\text{aq.})}^-$  : Electrical conductance

(D)  $Cl > F > Br > I$  : Electron affinity

9. (A), (B), (C)

Elements (a), (b) and (c) are correct. Statement (d) is incorrect as in any period, the atomic radius of the noble gas is largest.

10. (B), (C)

$$\frac{hc}{\lambda} = \phi + eV$$

V does not depend on intensity.

11. (B), (C), (D)

Aqueous tension depends only on T.

12. (D)

$$n \propto \frac{V}{T}$$

$$n_A : n_B = \frac{1}{2} : 2 = 1 : 4$$

$$n_B = \frac{4}{5} \times 15 = 12$$

13. (B)

$$n_A = 3 \text{ mole}$$

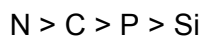
$$n_B : n_C = 2 : 1$$

$$n_B = \frac{2}{3} \times 12 = 8 \text{ mole}$$

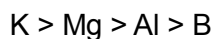
$$\text{Now, } P \propto \frac{nT}{V}$$

$$P_A : P_B = \frac{3 \times 2T}{V} : \frac{8 \times T}{2V} = \frac{3}{2}$$

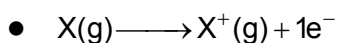
14. (B)



15. (D)

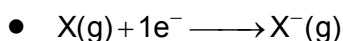


16. (B)



$$\frac{3N_0}{2} \quad E_1$$

$$\text{After loss of 1 electron} = \frac{E_1}{\frac{3N_0}{2}} = \frac{2E_1}{3N_0}$$



$$\frac{2N_0}{3} \quad E_2$$

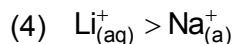
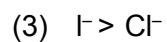
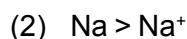
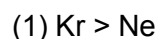
$$\text{After gain of 1 electron} = \frac{E_2}{\frac{2N_0}{3}} = \frac{3E_2}{2N_0}$$

17. (3)

$$\frac{V_1}{V_2} = \frac{K_1}{K_2} = \frac{\frac{hc}{50} - \frac{hc}{200}}{\frac{hc}{100} - \frac{hc}{200}} = \frac{3}{1} = 3$$

18. (4)

Atomic size



19. (2)

$$K.E_\alpha = 2\text{eV}, m_\alpha = 4\text{unit}$$

$$K.E_p = 32\text{eV}, m_p = 1\text{unit}$$

$$\lambda \propto \frac{1}{\sqrt{km}}$$

$$\frac{\lambda_{\alpha}}{\lambda_{\beta}} = \sqrt{\frac{32}{8}} = 2$$

20. (5)

6th excited state is 3d.

21. (4)

$$T_A = T$$

$$T_B = 20 T \quad (T \propto V, n, p \text{ constant})$$

$$T_C = 4T \quad (T \propto P, n, v \text{ constant})$$

22. (2)

Total Correct = 4 and

Total Incorrect = 2

So, Total =  $|4 - 2| = 2$ 

23. (2)

(v)  $\text{Li} < \text{Li}^+$  and (viii)  $\text{Ba} < \text{Sr}$ 

## PHYSICS

24. (A)

Block will start slipping when  $F = \mu mg$ 

$$2t = 0.5 \times 20 = 10$$

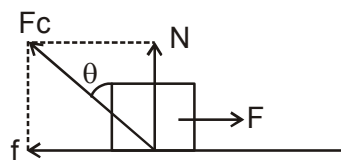
$$t = 5 \text{ s}$$

$$\text{for } t \leq 5 \text{ s, } \tan \theta = \frac{f}{N} = \frac{2t}{20} = \frac{t}{10}$$

$$\sec^2 \theta \frac{d\theta}{dt} = \frac{1}{10}, \frac{d\theta}{dt} = \frac{\cos^2 \theta}{10}$$

$$\text{At } t = 2 \text{ s, } \tan \theta = \frac{1}{5}$$

$$\cos \theta = \frac{5}{\sqrt{26}}$$



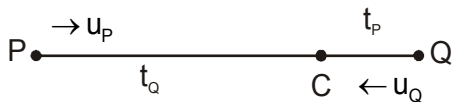
$$\frac{d\theta}{dt} = \frac{25}{260} = \frac{5}{52} \text{ rad/s}$$

25. (B)

$$T_1 = \frac{mg}{\cos \theta}, T_2 = mg \cos \theta$$

$$\frac{T_1}{T_2} = \sec^2 \theta = 4$$

26. (A)



Point C is point of crossing of buses.

Buses start from P and Q take same time to reach point C. Let this time is equal to 't'

$$u_p t = u_q t_q \quad \dots \text{ (i)}$$

$$u_q t = u_p t_p \quad \dots \text{ (ii)}$$

Dividing (i) & (ii)

$$\frac{u_p}{u_q} = \frac{u_q}{u_p} \cdot \frac{t_q}{t_p}$$

$$\frac{u_p^2}{u_q^2} = \frac{t_q}{t_p}$$

$$\therefore \frac{u_p}{u_q} = \sqrt{\frac{t_q}{t_p}}$$

27. Acceleration of blocks =  $\frac{(2M - m - M)g}{3M + m} = \frac{(M - m)g}{3M + m}$

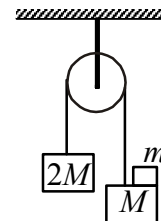
Considering free body diagram of block  $m$  only ,

$$mg + ma = N$$

$$N = m(g + a) = m \left[ g + \frac{(M - m)g}{3M + m} \right]$$

$$= m \frac{[3Mg + mg + Mg - mg]}{3M + m} = \frac{4Mmg}{3M + m}$$

$\therefore$  (B)



28. (D)

Let N be the normal reaction between m and M,

Equilibrium of M

$$N \sin 37^\circ = kx \quad \dots (i)$$

Equilibrium of m in vertical direction gives

$$N \cos 37^\circ = mg \quad \dots (ii)$$

From Eqs. (i) and (ii), we get

$$\tan 37^\circ = \frac{kx}{mg}$$

$$\frac{3}{4} = \frac{kx}{mg}$$

$$x = \frac{3mg}{4k}$$

29. (C)

$$\text{Given that : } \left| \vec{a}_1 + \vec{a}_2 \right| = \sqrt{3}$$

$$1 + 1 + 2 \cos \theta = (\sqrt{3})^2$$

$$2 \cos \theta = (3 - 2) = 1$$

$$\therefore \cos \theta = \frac{1}{2} \Rightarrow \theta = 60^\circ$$

$$\left( \vec{a}_1 - 2\vec{a}_2 \right) \cdot \vec{a}_1 = a_1^2 - 2\vec{a}_1 \cdot \vec{a}_2$$

$$\text{As } \vec{a}_1 \text{ and } \vec{a}_2 \text{ are unit vectors. Then, } \left( \vec{a}_1 - 2\vec{a}_2 \right) \cdot \vec{a}_1 = a_1^2 - 2\vec{a}_1 \cdot \vec{a}_2$$

$$= 1 - 2 \times 1 \times 1 \cos \theta$$

$$= 1 - 2 \cos \theta = 1 - 1 = 0.$$

30. (A)

$$\text{Let } \vec{b} = b_x \hat{i} + b_y \hat{j} + b_z \hat{k}.$$

As  $\vec{a}$  and  $\vec{b}$  are collinear

$$\text{So, } \frac{b_x}{2} = \frac{b_y}{1} = \frac{b_z}{-1} = k \text{ (Say)}$$

$$b_x = 2k, b_y = k, b_z = -k.$$

$$\text{As, } \vec{a} \cdot \vec{b} = 3 \Rightarrow (2k \times 2) + (k) + k = 3 \Rightarrow 6k = 3, \therefore k = \frac{1}{2}$$

Hence,  $\vec{b}$  is  $(1, \frac{1}{2}, -\frac{1}{2})$

**31. (A, B, C)**

$$T = 2g = 20 \text{ N}$$

frictional force = 0

$\therefore$  contact force = N

$$= 40 \frac{\sqrt{3}}{2}$$

$$= 20\sqrt{3} \text{ N}$$

normal to the inclined surface.

**32. (A), (D)**

Tension in  $S_1$  before cutting

$$T = 2 mg \sin 30^\circ = mg$$

So, Spring force  $F_s = 2T = 2mg$

just after cutting spring force will be same.

$$\text{So, } a_A = \frac{F_s}{m} = 2g$$

$$a_0 = g \sin 30^\circ = \frac{g}{2}$$

**33. Maximum acceleration of block  $A = \frac{0.5mg}{m} = \frac{g}{2}$**

So, if  $M = 2m$ ,  $a_A = a_B = \frac{2mg}{4m} = \frac{g}{2}$  and friction force is  $\frac{1}{2} mg$ .

$\therefore$  (A), (B), (C)



34. As  $\theta_1 = \tan^{-1}(\mu_1)$  and  $\theta_2 = \tan^{-1}(\mu_2) = 45^\circ = 30^\circ$

$\therefore$  If  $\theta < 30^\circ$ , there is no contact force between them.

For motion to start  $2 mg \sin \theta = (\mu_1 + \mu_2) mg \cos \theta$

$\therefore \tan \theta = \frac{\mu_1 + \mu_2}{2}$

(A), (C), (D)

35. (B)

to go up,  $t = \frac{60}{10} = 6\text{s}$

to come down,  $t = 6\text{ s}$

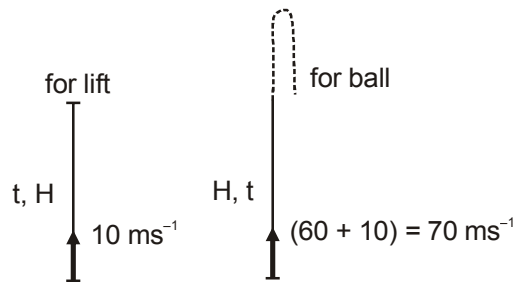
$\therefore T = 12\text{s}$

36. (A)

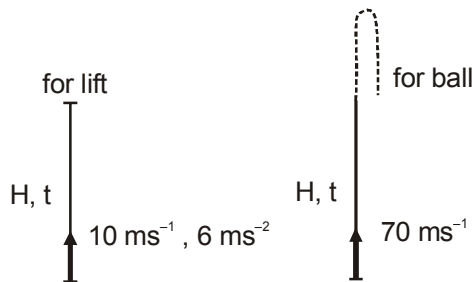
$\therefore 10t = 70t - \frac{1}{2} \times 10t^2$

$\therefore 5t^2 = 60t$

$\therefore t = 12\text{s}$



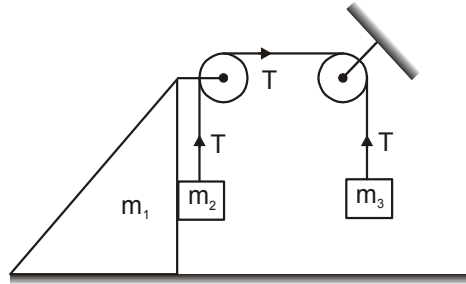
37. (C)



$10t + \frac{1}{2} \times 6t^2 = 70t - \frac{1}{2} \times 10t^2$

$8t^2 = 60t \Rightarrow t = \frac{60}{8} = 7.5\text{ sec.}$

38. (A)  
39. (B)



From constraint relation ;

$$Tx_1 + Tx_2 + Tx_3 = 0$$

by double diff<sup>n</sup>.

$$Ta_1 + Ta_2 + Ta_3 = 0$$

$$\therefore a_1 + a_2 + a_3 = 0 \quad \dots(A)$$

F.B.D. of wedge of mass  $m_1$  ;

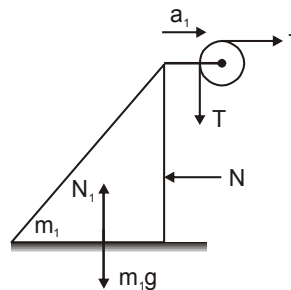
$$T - N = m_1 a_1$$

$$N = m_2 a_1$$

$$\therefore T = m_1 a_1 + m_2 a_1$$

$$= a_1(1 + 2) = 3a_1$$

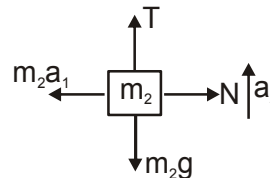
$$T = 3a_1 \quad \dots(i)$$



F.B.D. mass  $m_2$  ;

$$T - m_2 g = m_2 a_2$$

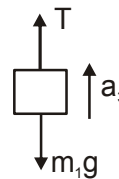
$$T - 2g = 2a_2 \quad \dots(ii)$$



F.B.D. of mass  $m_3$  ;

$$T - m_3 g = m_3 a_3$$

$$T - 3g = 3a_3 \quad \dots(iii)$$



From (i) , (ii) & (iii) and putting in equation (A)

$$\frac{T}{3} + \frac{T}{2} - g + \frac{T}{3} - g = 0$$

$$\frac{2T}{3} + \frac{T}{2} = 2g \Rightarrow \frac{4T + 3T}{6} = 2g$$

$$\Rightarrow T = \frac{6 \times 2 \times 10}{7} = \frac{120}{7} \text{ N}$$

$$a_1 = \frac{T}{3} = \frac{40}{7} \text{ ms}^{-2}$$

$$a_2 = \frac{T}{2} - g = \frac{60}{7} - 10 = \frac{-10}{7} \text{ ms}^{-2}$$

so, acc<sup>n</sup> of mass  $m_2$ ;

$$\sqrt{a_2^2 + a_1^2} = \sqrt{\left(\frac{40}{7}\right)^2 + \left(\frac{10}{7}\right)^2}$$

$$= \frac{10}{7} \sqrt{16+1} = \frac{\sqrt{17}}{7} g \text{ ms}^{-2}$$

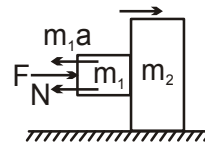
acc<sup>n</sup> of mass  $m_3$ ;

$$a_3 = \frac{T}{3} - g = \frac{40}{7} - 10$$

$$= -\frac{30}{7} \text{ ms}^{-2}$$

40. (5)

$$a = \left( \frac{F}{m_1 + m_2} \right)$$



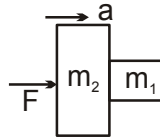
$$N + m_1 a = F \quad N = F - \frac{m_1 F}{m_1 + m_2}$$

$$N = \frac{m_2 F}{m_1 + m_2}$$

$$m_1 g = \frac{\mu m_2 F}{m_1 + m_2} \therefore \frac{m_1 (m_1 + m_2) g}{\mu m_2} = F_{\min}$$

for fig. (i)

$$\text{and } a = \frac{F}{m_1 + m_2}$$



$$N = m_1 a = \frac{m_1 F}{m_1 + m_2}$$

$$\therefore m_1 g = \frac{\mu m_1 F}{m_1 + m_2} \Rightarrow F = \frac{m_1(m_1 + m_2)g}{\mu m_1} \text{ for fig. (ii)}$$

$$\therefore \frac{(F_{\min})_{\text{fig.1}}}{(F_{\min})_{\text{fig.2}}} = \frac{m_1(m_1 + m_2)g}{\mu m_2} \times \frac{\mu m_1}{m_1(m_1 + m_2)g} = \frac{m_1}{m_2} = \frac{10}{2} = 5$$

41. (1)

$$I = \int_{\pi/4}^{\pi/2} (\sin x + \cos x) dx = [-\cos x]_{\pi/4}^{\pi/2} + [\sin x]_{\pi/4}^{\pi/2} = -[\cos \frac{\pi}{2} - \cos \frac{\pi}{4}] + [\sin \frac{\pi}{2} - \sin \frac{\pi}{4}]$$

$$= \cos \frac{\pi}{4} + \sin \frac{\pi}{2} - \sin \frac{\pi}{4} = 1$$

42. (5)

In the frame of the lift first pulley will be stationary so velocity of second pulley will be zero & Hence in the frame of ground it moves with 5 m/s

43. (4)

$$T = \frac{4m_1 m_2 m_3 g}{4m_1 m_2 + m_2 m_3 + m_1 m_3}$$

44. (6)

Force of friction between the two will be maximum i.e.,  $\mu mg$ .

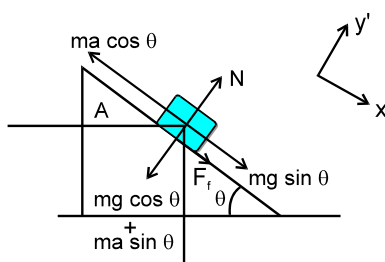
$$\text{Retardation of A is } a_A = \frac{\mu mg}{m} = \mu g$$

$$\text{and acceleration of B is } a_B = \frac{\mu mg}{2m} = \frac{\mu g}{2}$$

$\therefore$  Required acceleration = 6

45. (2)

FBD of block B w.r.t. wedge A, for maximum 'a' :



Perpendicular to wedge :

$$\Sigma f_y = (mg \cos \theta + m a \sin \theta - N) = 0.$$

$$\text{and } \Sigma f_x = mg \sin \theta + \mu N - ma \cos \theta = 0 \quad (\text{for maximum } a)$$

$$\Rightarrow mg \sin \theta + \mu(mg \cos \theta + ma \sin \theta) - ma \cos \theta = 0$$

$$\Rightarrow a = \frac{(g \sin \theta + \mu g \cos \theta)}{\cos \theta - \mu \sin \theta}$$

for  $\theta = 45^\circ$ 

$$a = g \left( \frac{\tan 45^\circ + \mu}{\cot 45^\circ - \mu} \right) ; \quad a = g \left( \frac{1 + \mu}{1 - \mu} \right) = 30$$

$$\text{hence, } \frac{60}{a} = 2$$

46. (8)

Since  $mg \sin 37^\circ > \mu mg \cos 37^\circ$ , the block has a tendency to slip downwards.

Let F be the minimum force applied on it, so that it does not slip. Then,

$$N = F + mg \cos 37^\circ$$

$$\therefore mg \sin 37^\circ = \mu N = \mu(F + mg \cos 37^\circ)$$

$$\text{or } F = \frac{mg \sin 37^\circ}{\mu} - mg \cos 37^\circ$$

$$= \frac{(2)(10)(3/5)}{0.5} - (2)(10)\left(\frac{4}{5}\right) = 8\text{N}$$

## CHEMISTRY

47. (C)

Since  $\log_x 9 = 2 \log_x 3$  the equation may be written  $2y^2 - 5y + 2 = 0$  where  $y = \log_x 3$

By the quadratic equation  $y = \frac{1}{2}$  or  $y = 2$  and hence  $x = 9$  or  $x = \sqrt{3}$ , which lies between 1 and 2.

$$2(\log_x 3)^2 - 5 \log_x 3 + 2 = 0 \quad \left\{ \begin{array}{l} t_1 \\ t_2 \end{array} \right.$$

$$t_1 t_2 = 1; \quad t_1 + t_2 = \frac{5}{2}$$

$$\log_{x_1} 3 + \log_{x_2} 3 = \frac{5}{2}$$

$$\frac{1}{\log_3 x_1} + \frac{1}{\log_3 x_2} = \frac{\log_3(x_1 x_2)}{1} = \frac{5}{2} \quad \Rightarrow \quad x_1 x_2 = 9\sqrt{3}$$

48. (D)

If exactly one - ve than  $E = 1$

exactly two - ve then  $E = -1$

all three - ve then  $E = -3$

all three + ve then  $E = 3$  ]

49. (C)

$$T_r = \frac{(r-1)r(r+1)}{r^3} = \frac{r-1}{r} \cdot \frac{r+1}{r}$$

$$\prod_{r=2}^n T_r = \left( \frac{1}{2} \cdot \frac{2}{3} \cdots \frac{n-2}{n-1} \cdot \frac{n-1}{n} \right) \left( \frac{3}{2} \cdot \frac{4}{3} \cdots \frac{n}{n-1} \cdot \frac{n+1}{n} \right) = \frac{n+1}{2n}$$

50. (B)

It is obvious

51. (B)

$$\text{LHS} = \frac{1}{2} [\sin A + \sin B + \sin C + \sin D] = 2 \quad \Rightarrow \quad \sum \sin A = 4$$

$$A = B = C = D = 90^\circ \quad \Rightarrow \quad \text{result}$$

52. (B)

$$\text{Let ratio be } \lambda : 1 \Rightarrow \frac{6\lambda - 3}{\lambda + 1} = 0, \lambda = \frac{1}{2}$$

53. (D)

54. (A,B,D)

$$\frac{\log x}{\log 3 + (1/2)\log x} + \frac{(1/2)\log x}{\log 3 + \log x} = 0; \quad \therefore \frac{\log_3 x}{1 + (1/2)\log_3 x} + \frac{1}{2} \frac{\log_3 x}{1 + \log_3 x} = 0$$

$$\text{let } \log_3 x = y$$

$$\frac{y}{1 + (y/2)} + \frac{y}{2(1+y)} = 0; \quad y \left( \frac{2}{2+y} + \frac{1}{2(1+y)} \right) = 0; \quad y[4 + 4y + 2 + y] = 0$$

$$\Rightarrow y = 0 \quad \text{or} \quad y = -6/5$$

$$\Rightarrow \log_3 x = 0 \quad \text{or} \quad \log_3 x = -6/5$$

$$x = 1 \quad \text{or} \quad x = 3^{-6/5}$$

$\Rightarrow$  A, B, D does not hold good. ]

55. (C,D)

$$\text{(A) } \sin \frac{3\pi}{8} \cos \frac{3\pi}{8} = \frac{1}{2} \sin \frac{3\pi}{4} = \frac{1}{2\sqrt{2}} = \text{irrational number.}$$

$$\text{(B) } \log_2 112 = \log_2 (2^4 \times 7) = 4 + \log_2 7 = \text{irrational number.}$$

$$\text{(C) } \log_3 2 \cdot \log_4 3 \cdot \log_8 4 = \frac{\log 2}{\log 3} \cdot \frac{\log 3}{\log 4} \cdot \frac{\log 4}{\log 8} = \log_8 2 = \frac{1}{3} = \text{rational number}$$

$$\text{(D) } 27^{-(\log_{125} 5)} = 27^{-(\log_{5^{-3}} 5)} = 27^{-\frac{1}{3}} = \frac{1}{3} = \text{rational number}$$

$\Rightarrow$  options (C) & (D) are correct ]

56. (A,B,D)

(C) in 'C' if the sign is (-) ve instead of (+) ve then the answer is 1 ]

57. (A,B,C,D)

Equation of line through A(4, 3) is

$$\frac{x-4}{\cos \theta} = \frac{y-3}{\sin \theta} = r \quad \dots\dots(i)$$

$$A \equiv (4 + r\cos\theta, 3 + r\sin\theta).$$

$$4 + r\cos\theta = 8 \Rightarrow r = 4 \sec \theta.$$

$$\therefore AB = 4 \sec\theta.$$

Similarly  $AC = 3 \operatorname{cosec} \theta$

$$\frac{16}{AB^2} + \frac{9}{AC^2} = \cos^2 \theta + \sin^2 \theta = 1$$

$$\text{So } AB + AC = \frac{4}{\cos \theta} + \frac{3}{\sin \theta} = \frac{2(4 \sin \theta + 3 \cos \theta)}{\sin 2\theta}$$

58. (C)

59. (B)

60. (C)

61. (D)

$$OA = 8 + \cot \theta ; OB = 1 + 8 \tan \theta$$

$$\begin{aligned} \Delta &= \frac{1}{2} (1 + 8 \tan \theta)(8 + \cot \theta) \\ &= 8 + \frac{1}{2} (64 \tan \theta + \cot \theta) \end{aligned}$$

For  $\Delta$  to be minimum  $\tan \theta = 1/8$

$$\therefore \Delta_{\min} = 16$$

62. (A)

$$z = AB = \operatorname{cosec} \theta + 8 \sec \theta \Rightarrow \frac{dz}{d\theta} = 0 ; \cot \theta = 2$$

$$\therefore AB_{\min} = 5\sqrt{5}$$

63. (1)

$$\text{Either } x = y \text{ or } x = \left| \frac{3x + 4y - 12}{5} \right| \text{ or } y = \left| \frac{3x + 4y - 12}{15} \right| \Rightarrow (1, 1)$$

64. (6)

$$\log_8(kx^2 + wx + f) = 2 \Rightarrow kx^2 + wx + f = 64$$

$$\therefore kx^2 + wx + f - 64 = 0 \quad \dots(1)$$

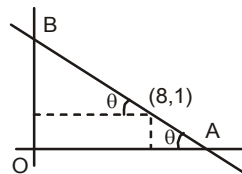
also (1) is identical to  $(3x - 1)(x + 15)$

$$\therefore kx^2 + wx + f - 64 = 3x^2 + 44x - 15$$

$$k = 3; w = 44 \text{ and } f - 64 = -15$$

$$k = 3, w = 44 \text{ and } f = 49$$

$$\therefore k + w + f = 96$$





65. (4)

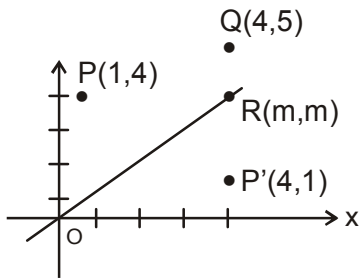


Image of (1, 4) about the line  $y = x$  is (4, 1)  $\Rightarrow$  P'(4,1) Q(4,5) and R(m, m) are collinear.

$$\Rightarrow m = 4$$

66. (5)

$$a - d + a + a + d = 10$$

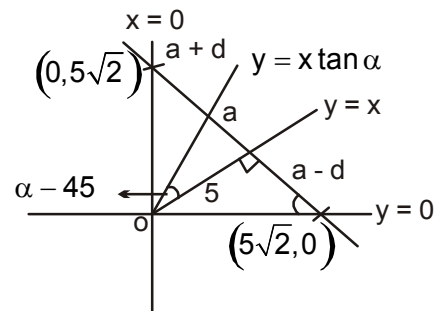
$$a = \frac{10}{3}$$

$$\therefore a - d = 5$$

$$\tan(\alpha - 45^\circ) = \frac{a}{5}$$

$$\frac{\tan \alpha - 1}{\tan \alpha + 1} = \frac{2}{3} \Rightarrow 3 \tan \alpha - 3 = 2 \tan \alpha + 2$$

$$\tan \alpha = 5$$



67. (4)

$$\text{Let } \theta = \frac{\pi}{16}; \quad 8\theta = \frac{\pi}{2}$$

$$\therefore y = \tan \theta + \tan 5\theta + \tan 9\theta + \tan 13\theta$$

$$\therefore y = (\tan \theta - \cot \theta) + (\tan 5\theta - \cot 5\theta)$$

$$[ \tan 13\theta = \tan(8\theta + 5\theta) = -\cot 5\theta; \tan 9\theta = \tan(8\theta + \theta) = -\cot \theta ]$$

$$= (\tan \theta - \cot \theta) + (\cot 5\theta - \tan 5\theta)$$

$$= \frac{\sin^2 \theta - \cos^2 \theta}{\sin \theta \cos \theta} + \frac{\cos^2 5\theta - \sin^2 5\theta}{\sin 5\theta \cos 5\theta}$$

$$y = -2 \cdot \frac{\sin 4\theta}{\cos 2\theta \sin 2\theta} = -4$$

Hence absolute value = 4 Ans.]

68. (0)

$$\begin{vmatrix} \lambda_1 & 2a\lambda_1 + \lambda_1^3 & 1 \\ \lambda_2 & 2a\lambda_2 + \lambda_2^3 & 1 \\ \lambda_3 & 2a\lambda_3 + \lambda_3^3 & 1 \end{vmatrix} = 0$$

$$\Rightarrow a(\lambda_1 - \lambda_2)(\lambda_2 - \lambda_3)(\lambda_3 - \lambda_1)(\lambda_1 + \lambda_2 + \lambda_3) = 0$$

But  $a \neq 0$ ,  $\lambda_1 \neq \lambda_2 \neq \lambda_3$

$$\therefore \lambda_1 + \lambda_2 + \lambda_3 = 0.$$

69. (5)

$$\frac{4\log_2 \sqrt{x}}{\log_2(x/2)} + \frac{2\log_2(x^2)}{\log_2(4x)} = \frac{3\log_2(x^3)}{\log_2(2x)}$$

$$\frac{4 \cdot \frac{1}{2} \log_2(x)}{\log_2 x - 1} + \frac{4\log_2(x)}{2 + \log_2(x)} = \frac{9\log_2(x)}{1 + \log_2(x)}$$

let  $\log_2 x = t$

$$\frac{2t}{t-1} + \frac{4t}{t+2} = \frac{9t}{t+1} \quad (\text{hence either } t = 0)$$

$$\text{or } \frac{2}{t-1} + \frac{4}{t+2} = \frac{9}{t+1} \Rightarrow \frac{2t+4+4t-4}{(t-1)(t+2)} = \frac{9}{t+1} \Rightarrow 6t(t+1) = 9(t^2+t-2)$$

$$\Rightarrow 6t^2 + 6t = 9t^2 + 9t - 18 \Rightarrow 3t^2 + 3t - 18 = 0 \Rightarrow t^2 + t - 6 = 0 \Rightarrow (t+3)(t-2) = 0$$

hence  $t = 0$ ,  $t = 2$  &  $t = -3$ ,

$x = 1$ ,  $x = 4$ ,  $x = 1/8$  (rejected  $\because$  it is not integral value)]