

SOLUTIONS

PROGRESS TEST-1

GZ-1919 To 1921

GZK-1906

JEE MAIN PATTERN

Test Date: 29-07-2017



Corporate Office: Paruslok, Boring Road Crossing, Patna-01
Kankarbagh Office: A-10, 1st Floor, Patrakar Nagar, Patna-20
Bazar Samiti Office : Rainbow Tower, Sai Complex, Rampur Rd.,
Bazar Samiti Patna-06
Call : 9569668800 | 7544015993/4/6/7

PHYSICS

1. (C)
sum of three non coplanar vectors can not be zero
2. (A)
3. (A)
4. (A)
5. (D)
6. (D)
7. (A)
8. (D)
9. (A)

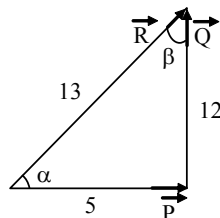
$$\vec{C} = \vec{A} + \vec{B} = (3\hat{i} + 6\hat{j} - 2\hat{k})$$

$$\hat{C} = \frac{\vec{C}}{|\vec{C}|} = \frac{3\hat{i} + 6\hat{j} - 2\hat{k}}{\sqrt{3^2 + 6^2 + (-2)^2}} = \frac{3\hat{i} + 6\hat{j} - 2\hat{k}}{7}$$

10. (C)

$$\cos \beta = \frac{12}{13}$$

$$\therefore \beta = \cos^{-1} \left(\frac{12}{13} \right)$$



11. (C)

$$\frac{|\vec{R}|_{\min}}{|\vec{R}|_{\max}} = \frac{1}{4} = \frac{||\vec{A}| - |\vec{B}||}{|\vec{A}| + |\vec{B}|}$$

$$|\vec{A}| + |\vec{B}| = 4 ||\vec{A}| - |\vec{B}||$$

If $|\vec{A}| > |\vec{B}|$

$$|\vec{A}| + |\vec{B}| = 4 (|\vec{A}| - |\vec{B}|)$$

$$3|\vec{A}| = 5|\vec{B}| \Rightarrow \frac{|\vec{A}|}{|\vec{B}|} = \frac{5}{3}$$

If $|\vec{B}| > |\vec{A}|$

$$|\vec{A}| + |\vec{B}| = 4 (|\vec{B}| - |\vec{A}|)$$

$$\frac{|\vec{A}|}{|\vec{B}|} = \frac{3}{5}$$

12. (D)

$$\therefore |\vec{F}_1 + \vec{F}_2| = P$$

$$\Rightarrow F_1^2 + F_2^2 + 2F_1F_2 \cos\theta = P^2 \quad \dots(1)$$

$$\& |\vec{F}_1 - \vec{F}_2| = Q$$

$$\Rightarrow F_1^2 + F_2^2 - 2F_1F_2 \cos\theta = Q^2 \quad \dots(2)$$

$$(1) + (2), \quad \boxed{2(F_1^2 + F_2^2) = P^2 + Q^2}$$

13. (D)

14. (A)

15. (A)

$$\text{Component of } \vec{A} \text{ along } \vec{B} = \frac{\vec{A} \cdot \vec{B}}{|\vec{B}|} \cdot \hat{B}$$

16. (A)

17. (D)

$$\vec{a} = 3\hat{i} + 4\hat{j}. \text{ Let } \vec{c} = c_x\hat{i} + c_y\hat{j}, \quad \vec{c} \text{ is perpendicular to } \vec{a} \quad \therefore 3c_x + 4c_y = 0$$

$$c_y = -\frac{3}{4}c_x \quad (i)$$

$$|\vec{c}| = 5, \quad c_x^2 + c_y^2 = 25, \quad c_x^2 + \frac{9c_x^2}{16} = 25,$$

$$c_x = \pm 4, \quad \therefore c_y = \mp 3$$

18. (A)

19. (B)

20. (D)

21. (B)

$$\begin{aligned} & |\vec{a} - \vec{b}|^2 + |\vec{b} - \vec{c}|^2 + |\vec{c} - \vec{a}|^2 \\ &= (\vec{a} - \vec{b}) \cdot (\vec{a} - \vec{b}) + (\vec{b} - \vec{c}) \cdot (\vec{b} - \vec{c}) + (\vec{c} - \vec{a}) \cdot (\vec{c} - \vec{a}) \\ &= a^2 + b^2 - 2\vec{a} \cdot \vec{b} + b^2 + c^2 - 2\vec{b} \cdot \vec{c} + c^2 + a^2 - 2\vec{c} \cdot \vec{a} \\ &= 2(a^2 + b^2 + c^2) - 2(\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a}) \end{aligned}$$

Now, as

$$|\vec{a} + \vec{b} + \vec{c}|^2 = a^2 + b^2 + c^2 + 2(\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a}) \geq 0$$

$$\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a} \geq -\frac{3}{2}$$

for maximum value of

$$|\vec{a} - \vec{b}|^2 + |\vec{b} - \vec{c}|^2 + |\vec{c} - \vec{a}|^2$$

the minimum value of $\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a}$ should be taken.

So, $2(1+1+1) - 2 \times \left(\frac{-3}{2}\right) = 9$ is the maximum value of $|\vec{a} - \vec{b}|^2 + |\vec{b} - \vec{c}|^2 + |\vec{c} - \vec{a}|^2$

- | | | | |
|---------|---------|---------|---------|
| 22. (C) | 23. (A) | 24. (B) | 25. (B) |
| 26. (D) | 27. (D) | 28. (A) | 29. (A) |
| 30. (C) | | | |

CHEMISTRY

31. (C)

$$\text{moles} = \frac{g}{M_0} = \frac{54}{124} = 0.4355$$

32. (C)

$$\text{Number of moles of magnesium} = \frac{0.004}{24} = \frac{1}{6} \times 10^{-3}$$

$$\begin{aligned} \therefore \text{Total number of atoms} &= \frac{1}{6} \times 10^{-3} \times N_A \\ &= \frac{1}{6} \times 10^{-3} \times 6.022 \times 10^{23} \\ &\approx 10^{20} \text{ atoms} \end{aligned}$$

33. (D)

1 mole of electron contains N_A electrons.

$$\begin{aligned} \therefore \text{Weight of 1 mole of electrons} \\ &= 6.022 \times 10^{23} \times 9 \times 10^{-28} \\ &= 0.00054 \text{ gm} \end{aligned}$$

34. (B)

(A) 50 grams of iron

(B) Mass of Nitrogen (N_2) = $5 \times 28 = 140$ g

(C) 1 gram atom of silver means 1 mole of silver

$$\therefore \text{Mass of silver atom} = 1 \times 108 = 108 \text{ g}$$

(D) Number of moles of C = $\frac{5 \times 10^{23}}{6.022 \times 10^{23}} = 0.83$

$$\therefore \text{Mass of C} = \text{Number of moles} \times 12 = 0.83 \times 12 = 9.96 \text{ g}$$

So, option (B) has highest mass.

35. (D)

$$\text{Moles of gas} = \frac{5.6}{22.4} = \frac{1}{4}$$

$$\text{Number of moles} = \frac{\text{weight}}{\text{GMM}}$$

$$\Rightarrow \frac{1}{4} = \frac{11}{\text{GMM}}$$

$$\Rightarrow \text{GMM} = 44 \text{ g/mol}$$

∴ The gas is N₂O (Nitrous oxide)

36. (B)

Let the natural abundance of ⁶³Cu be x% and the natural abundance of ⁶⁵Cu be (100 – x) %

$$\text{Average atomic mass of Copper} = \frac{\text{At. weight of 1}^{\text{st}} \text{ isotope} \times \% + \text{At. weight of 2}^{\text{nd}} \text{ Isotope} \times \%}{100}$$

$$\Rightarrow 63.6 = \frac{63 \times x + 65 \times (100 - x)}{100}$$

$$\Rightarrow 6360 = 63x + 6500 - 65x$$

$$\Rightarrow 2x = 140$$

$$\Rightarrow x = 70\%$$

37. (B)

X₂Y₃ → Pure Compound

Let the atomic weight of X be A_x and atomic weight of Y and A_y

$$\% \text{ of X} \Rightarrow \frac{2A_x}{2A_x + 3A_y} \times 100 = 60$$

$$\Rightarrow 200A_x = 120A_x + 180A_y$$

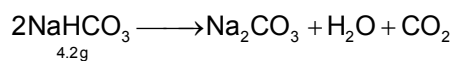
$$\Rightarrow 80A_x = 180A_y$$

$$\Rightarrow A_y = \frac{80}{180}A_x = \frac{4}{9}A_x$$

38. (C)

Empirical formula represents the simple ratio of atoms in a compound.

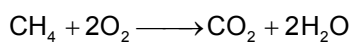
39. (D)



Number of moles of $\text{NaHCO}_3 = \frac{4.2}{84} = \frac{1}{20}$, No of moles of $\text{CO}_2 = 1/20 \times 1/2 = 1/40$

So, Volume of CO_2 formed at NTP $= \frac{1}{40} \times 22.4$
 $= 0.56 \text{ L}$

40. (A)



1 L at NTP

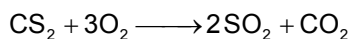
$$n_{\text{CH}_4} = \frac{1}{22.4}$$

A/c to mole – mole analysis

$$\frac{n_{\text{CH}_4}}{1} = \frac{n_{\text{O}_2}}{2} \Rightarrow n_{\text{O}_2} = 2 \times \frac{1}{22.4}$$

$\therefore V_{\text{O}_2}$ at NTP $= \frac{2}{22.4} \times 22.4 = 2 \text{ L}$.

41. (D)



(A) 1 mole of CS_2 will produce 1 mole of CO_2

(True Statement)

$$(B) n_{\text{O}_2} = \frac{16}{32} = \frac{1}{2}$$

A/c to mole – mole analysis

$$\frac{n_{\text{O}_2}}{3} = \frac{n_{\text{CO}_2}}{1} \Rightarrow n_{\text{CO}_2} = \frac{1}{6}$$

So, mass of $\text{CO}_2 = \frac{44}{6} = 7.33 \text{ g}$. (True)

(C) A/c to mole – mole analysis

$$\frac{n_{\text{O}_2}}{3} = \frac{n_{\text{SO}_2}}{2} \Rightarrow n_{\text{SO}_2} = \frac{2}{3} \text{ (True)}$$

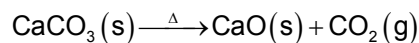
$$(D) n_{\text{O}_2} = \frac{6}{N_A}$$

A/c to mole – mole analysis

$$\frac{n_{O_2}}{3} = \frac{n_{CS_2}}{1} \Rightarrow n_{CS_2} = \frac{6}{N_A} \times \frac{1}{3}$$

\therefore No. of molecules of $CS_2 = \frac{2}{N_A} \times N_A = 2$. (False)

42. (C)



5.6 L at NTP

$$n_{CO_2} = \frac{5.6}{22.4} = \frac{1}{4}$$

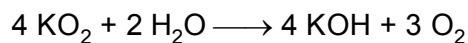
A/c to mole – mole analysis

$$\frac{n_{CaO}}{1} = \frac{n_{CO_2}}{1}$$

$$\Rightarrow n_{CaO} = \frac{1}{4}$$

\therefore mass of $CaO = \frac{1}{4} \times 56 = 14$ gm.

43. (B)



0.158 0.1

L.R. = KO_2

\therefore No. of moles of O_2 formed = $\frac{3}{4} \times 0.158 = 0.1185$ mole

44. (A)

$$\% \text{ of 'B'} = \frac{3B}{2A + 3B} \times 100 = \frac{3 \times (1.5A)}{2A + 3 \times (1.5A)} \times 100 = \frac{4.5}{6.5} \times 100 = 69.2\%$$

45. (C)

$$\frac{n_O}{n_B} = \frac{y}{3} = \frac{1}{0.3} \Rightarrow y = 10$$

$$\frac{n_H}{n_A} = \frac{4}{1} = \frac{2y}{x} = \frac{2 \times 10}{x} \Rightarrow x = 5$$

46. (B)

$$\% C = \frac{72}{180} \times 50 = 20\%$$

47. (C)

$$M_{av} = \frac{4 \times 80 + 2 \times 28}{6} = \frac{320 + 56}{6} = \frac{376}{6} = 62.66$$

$$(V.D.)_{av} = \frac{M_{av}}{2} = \frac{62.66}{2} = 31.33$$

48. (A)

$$(I) \quad 0.5 \text{ mole of } O_3 = 0.5 \times 48 = 24 \text{ gm}$$

$$(II) \quad 0.5 \text{ mole of 'O' } = 8 \text{ gm}$$

$$(III) \quad \frac{1}{2} \text{ mole of } O_2 = 16 \text{ gm}$$

$$(IV) \quad 0.25 \text{ mole of } CO_2 = 11 \text{ gm}$$

$$(I) > (III) > (IV) > (II)$$

49. (D)

$$40 = \frac{32a + 80b}{a + b}$$

$$40a + 40b = 32a + 80b$$

$$a = 5b$$

$$M_{av} = \frac{32b + 80a}{a + b}$$

$$= \frac{32b + 400b}{5b + b}$$

$$= \frac{432}{6} = 72$$

50. (B)



$$12\text{gm} \quad \quad \quad 16\text{gm}$$

$$6\text{mole} \quad \quad \quad 0.5\text{mole}$$

$$5\text{mole left} \quad \quad \quad \text{LR}$$

$$10\text{g left.}$$

51. (D)

$$\text{Molecular weight of mixture} = \frac{40 \times 28 + 40 \times 32 + 20 \times 44}{100} = 32.8 \text{ g}$$

52. (C)

C ball 1400 can be used for 700

H ball 3600 can be used for 600

O ball 1000 can be used for 1000

Max possible is 600

53. (A)

Wt of carbon 1×10^{-6} gm

Mole of carbon = $1 \times 10^{-6} / 12$

$$\text{Atom of carbon} = \frac{0.000001 \times 6.023 \times 10^{23}}{12} = 5 \times 10^{16}$$

54. (A)

$$16.12 = \frac{90 \times 16 + x \times 17 + (100 - x) \times 18}{100}$$

$$x = 8$$

55. (A)

$$\text{Molecular weight} = \frac{4 \times 24 \times 100}{0.096} = 100000$$

56. (D)

Mole of glucose = $54/180 = 0.3$

Mole of CO_2 is $6 \times 0.3 = 1.8 = 1.8 \times 44 = 79.2\text{g}$

57. (A)

$$n_{\text{O}_2} = \frac{16}{32} = \frac{1}{2} \quad \& \quad n_{\text{N}_2} = \frac{14}{28} = \frac{1}{2}$$

58. (C)

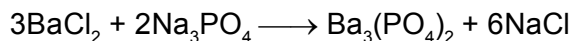
O_2 is the limiting reagent

59. (B)

$$1 \times n_{\text{CO}_2} = 6 \times n_{\text{K}_4[\text{Fe}(\text{CN})_6]}$$

$$\therefore n_{\text{K}_4[\text{Fe}(\text{CN})_6]} = \frac{1}{6}$$

60. (C)



Here BaCl_2 is the limiting reactant number of moles of $\text{Ba}_3(\text{PO}_4)_2$ formed

$$= \frac{1}{3} \times \text{No. of moles of } \text{BaCl}_2 = \frac{2}{3} \text{ mol.}$$

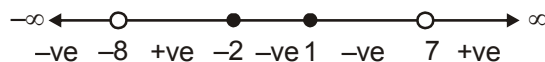
MATHEMATICS

61. (D)

$$|x| \left(\frac{1+|x|}{x^2-x+1} \right) \leq 0 \Rightarrow x=0$$

62. (B)

Using wavy curve method :



$$\therefore x \in (-\infty, 8) \cup [-2, 1] \cup [1, 7)$$

$$\text{i.e., } x \in (-\infty, 8) \cup [-2, 7)$$

63. (A)

64. (B)

$$\frac{(x-3)^3}{(x-4)(x-1)(\sqrt{2}-x)(\sqrt{2}+x)} \leq 0$$

$$x \in (-\sqrt{2}, 1) \cup (\sqrt{2}, 3] \cup (4, \infty)$$

65. (A)

Let x be the required logarithm, then by definition

$$(2\sqrt{2})^x = 32\sqrt[5]{4} \Rightarrow (2, 2^{1/2})^x = 2^5 \cdot 2^{2/5}, \therefore 2^{\frac{3x}{2}} = 2^{5+\frac{2}{5}}$$

$$\text{Here, by equating the indices, } \frac{3}{2}x = \frac{27}{5}$$

$$\therefore x = \frac{18}{5} = 3.6.$$

66. (B)

$$\log_{49} 28 = \frac{\log 28}{\log 49} = \frac{\log 7 + \log 4}{2\log 7}$$

$$= \frac{\log 7}{2\log 7} + \frac{\log 4}{2\log 7} = \frac{1}{2} + \frac{1}{2} \log_7 4 = \frac{1}{2} + \frac{1}{2} \cdot 2\log_7 2 = \frac{1}{2} + \log_7 2 = \frac{1}{2} + m = \frac{1+2m}{2}$$

67. (A)

$$\log_e \left(\frac{a+b}{2} \right) = \frac{1}{2} (\log_e a + \log_e b) = \frac{1}{2} \log_e (ab) = \log_e \sqrt{ab}$$

$$\Rightarrow \frac{a+b}{2} = \sqrt{ab} \Rightarrow a+b = 2\sqrt{ab} \Rightarrow (\sqrt{a} - \sqrt{b})^2 = 0 \Rightarrow \sqrt{a} - \sqrt{b} = 0 \Rightarrow a = b.$$

68. (D)

$$\text{If } \log_4 2 + \log_4 4 + \log_4 16 + \log_4 x = 6$$

$$\text{then } \log_4 (2 \times 4 \times 16 \times x) = 6$$

$$\Rightarrow \log_4 128x = 6 \Rightarrow 128x = 4^6 \Rightarrow x = \frac{64 \times 64}{128} \Rightarrow x = 32$$

69. (C)

$$a = \log_{24} 12 = \frac{\log 12}{\log 24} = \frac{2\log 2 + \log 3}{3\log 2 + \log 3}$$

$$b = \log_{36} 24 = \frac{3\log 2 + \log 3}{2(\log 2 + \log 3)}$$

$$c = \log_{48} 36 = \frac{2(\log 2 + \log 3)}{4\log 2 + \log 3}$$

$$\therefore abc = \frac{2\log 2 + \log 3}{4\log 2 + \log 3}$$

$$\Rightarrow 1 + abc = \frac{6\log 2 + 2\log 3}{4\log 2 + \log 3} = 2 \cdot \frac{3\log 2 + \log 3}{4\log 2 + \log 3} = 2bc.$$

70. (B)

$$2^{\log_{\sqrt{2}}(x-1)} > x + 5 \Rightarrow (\sqrt{2})^{2\log_{\sqrt{2}}(x-1)} > x + 5$$

$$\Rightarrow (x-1)^2 > x + 5 \Rightarrow x^2 - 3x - 4 > 0 \Rightarrow (x-4)(x+1) > 0 \Rightarrow x > 4 \text{ or } x < -1$$

But for $\log_{\sqrt{2}}(x-1)$ to be defined $x-1 > 0$

i.e., $x > 1$

$$\therefore x > 4 \Rightarrow x \in (4, \infty).$$

71. (C)

$$\log_{0.04}(x-1) \geq \log_{0.2}(x-1) \quad \dots\dots(i)$$

For log to be defined $x-1 > 0 \Rightarrow x > 1$

$$\text{From (i), } \log_{(0.2)^2}(x-1) \geq \log_{0.2}(x-1)$$

$$\Rightarrow \frac{1}{2} \log_{0.2}(x-1) \geq \log_{0.2}(x-1) \Rightarrow \sqrt{x-1} \leq (x-1)$$

$$\Rightarrow \sqrt{x-1}(1-\sqrt{x-1}) \leq 0 \Rightarrow 1-\sqrt{x-1} \leq 0$$

$$\Rightarrow \sqrt{x-1} \geq 1 \Rightarrow x \geq 2, \therefore x \in [2, \infty).$$

72. (B)

Since $x^2 + 1 = 0$, gives $x^2 = -1 \Rightarrow x = \pm i$

$\therefore x$ is not real but x is real (given)

\therefore No value of x is possible.

73. (B)

$$A = [x : x \in \mathbb{R}, -1 < x < 1]$$

$$B = [x : x \in \mathbb{R} : x-1 \leq -1 \text{ or } x-1 \geq 1]$$

$$= [x : x \in \mathbb{R} : x \leq 0 \text{ or } x \geq 2]$$

$\therefore A \cup B = \mathbb{R} - D$, where

$$D = [x : x \in \mathbb{R}, 1 \leq x < 2].$$

74. (B)

$$n(A \cap B) = n(A) + n(B) - n(A \cup B) = 5$$

$$n(A - B) = n(A) - n(A \cap B) = 11$$

75. (A)

$$A \cup B = \{1, 2, 3, 4, 5, 6\} \therefore (A \cup B) \cap C = \{3, 4, 6\}.$$

76. (C) Since $x = 0$ is one of the solution so the product will be zero.77. (D) $|x^2 - 9| + |x^2 - 4| = 5$

$$|x^2 - 9| + |x^2 - 4| = |(x^2 - 9) - (x^2 - 4)|$$

$$\Rightarrow (x^2 - 9)(x^2 - 4) \leq 0 \{ \therefore |a| + |b| = |a - b| \Leftrightarrow a \cdot b \leq 0 \}$$

$$\Rightarrow x \in [-3, -2] \cup [2, 3]$$

78. (D)

Case I when $x \geq -2$

$$\frac{|x+2|-x}{2} < 2 \Rightarrow \frac{2}{x} < 2 \Rightarrow \frac{1}{x} < 1 \Rightarrow (x-1)/x > 0$$

$$x \in [-2, 0) \cup (1, \infty) \quad \dots(i)$$

Case II when $x < -2$

$$\frac{|x+2|-x}{x} < 2 \Rightarrow \frac{-2-2x}{x} < 2 \Rightarrow \frac{1+x}{x} + 1 > 0$$

$$\Rightarrow (1+2x)/x > 0 \Rightarrow x \in (-\infty, -2) \dots(ii)$$

\therefore from (i) and (ii) we get $x \in (-\infty, 0) \cup (1, \infty)$

79. (A) $|a| + |b| = |a - b|$

$$\Rightarrow ab \leq 0$$

$$(x^2 - 5x + 7)(x^2 - 5x - 14) \leq 0$$

$$(x - 7)(x + 2) \leq 0$$

$$\Rightarrow x \in [-2, 7]$$

80. (C) Use $A^{\log_a B} = B$

$$e^{\ell n(\ell n 3)} = \ell n 3$$

$$\therefore e^{e^{\ell n(\ell n 3)}} = e^{\ell n 3} = 3$$

81. (A)

$$N = \frac{(3^4)^{\log_3 5} + 3^{3 \log_3 \sqrt{6}}}{409} [7^{\log_7} - (5^3)^{\log_5 2^6}]$$

$$N = \frac{3^{\log_3 25} + 3^{\log_3 \sqrt{6}^3}}{409} [25 - 6\sqrt{6}]$$

$$N = \frac{(25 + 6\sqrt{6})(25 - 6\sqrt{6})}{409}$$

$$N = 1$$

$$\log_2 N = \log_2 1 = 0$$

82. (C)

$$x^2 + 3x + 2 \geq 0 \Rightarrow (x+1)(x+2) \geq 0$$

$$\Rightarrow x \in (-\infty, -2] \cup [-1, \infty)$$

Case I. $x - 1 < 0 \Rightarrow x < 1, x - 1 < \sqrt{x^2 + 3x + 2}$ is true

$$\therefore x \in (-\infty, -2] \cup [-1, 1) \quad \dots (i)$$

Case II. if $x - 1 \geq 0 \Rightarrow x \geq 1$

$$x - 1 < \sqrt{x^2 + 3x + 2}$$

$$\Rightarrow x^2 - 2x + 1 < x^2 + 3x + 2 \Rightarrow 5x + 1 > 0 \Rightarrow x > -\frac{1}{5}$$

$$\therefore x \in [1, \infty) \quad \dots (ii)$$

From (i) and (ii)

$$x \in (-\infty, -2] \cup [-1, \infty)$$

83. (D)

Using wavy curve method and the fact that $x = 0$ and 3 are the repeated roots of

$x(e^x - 1)(x + 2)(x - 3)^2 \leq 0$ we get the sign scheme of the given expression as

$$\begin{array}{ccccccc} & - & + & + & + & & \\ & | & | & | & | & & \\ & -2 & 0 & 3 & & & \end{array}$$

Thus complete solution is $x \in (-\infty, -2] \cup \{0, 3\}$

84. (D)

$$1 \leq |3 - x| < 2$$

and

$$|3 - x| \geq 1 \quad | \quad |3 - x| < 2$$

$$\Rightarrow x \in (-\infty, 2] \cup [4, \infty)$$

$$\Rightarrow x \in (1, 5)$$

Ans. $x \in (1, 2] \cup [4, 5)$

85. (C)

$$|x - 1| - |x - 2| = \frac{1}{2}$$

$$x \leq 1$$

$$-(x - 1) + (x - 2) = \frac{1}{2}$$

$$-1 = \frac{1}{2}$$

x

$$1 \leq x \leq 2$$

$$(x - 1) + (x - 2) = \frac{1}{2}$$

$$x = \frac{7}{4}$$

✓

$$x \geq 2$$

$$(x - 1) - (x - 2) = \frac{1}{2}$$

$$1 = \frac{1}{2}$$

x

86. (B)

$$3x^2 - 10x + 3 = 0 \Rightarrow x = 3, 1/3$$

$$\text{or, } |x - 4| = 1 \Rightarrow x = 5, 3.$$

87. (B)

$$|x - 1| \leq 2 \Rightarrow -2 \leq x - 1 \leq 2$$

$$\Rightarrow -1 \leq x \leq 3$$

88. (D)

$$\text{We have, } 5x + 2 < 3x + 8 \text{ and } \frac{x+2}{x-1} < 4 \Rightarrow 2x - 6 < 0 \text{ and } \frac{x+2}{x-1} - 4 < 0$$

$$\Rightarrow 2(x-3) < 0 \text{ and } \frac{-3x+6}{x-1} < 0 \Rightarrow x-3 < 0 \text{ and } \frac{x-2}{x-1} > 0$$

$$\Rightarrow x \in (-\infty, 3) \text{ and } x \in (-\infty, 1) \cup (2, \infty) \Rightarrow x \in (-\infty, 1) \cup (2, 3)$$

89. (C)

$$\frac{4 - 4x + 2 + 2x}{(1+x)(1-x)} - 1 < 0 \Rightarrow \frac{6 - 2x - 1 + x^2}{(1+x)(1-x)} < 0 \Rightarrow \frac{x^2 - 2x + 5}{(x+1)(x-1)} > 0$$

$$\Rightarrow \frac{1}{(x+1)(x-1)} > 0$$

90. (C)

$$x - 1 = x^2 - x = 0 \Rightarrow x = 1$$